

Name:

Section:

Student No:

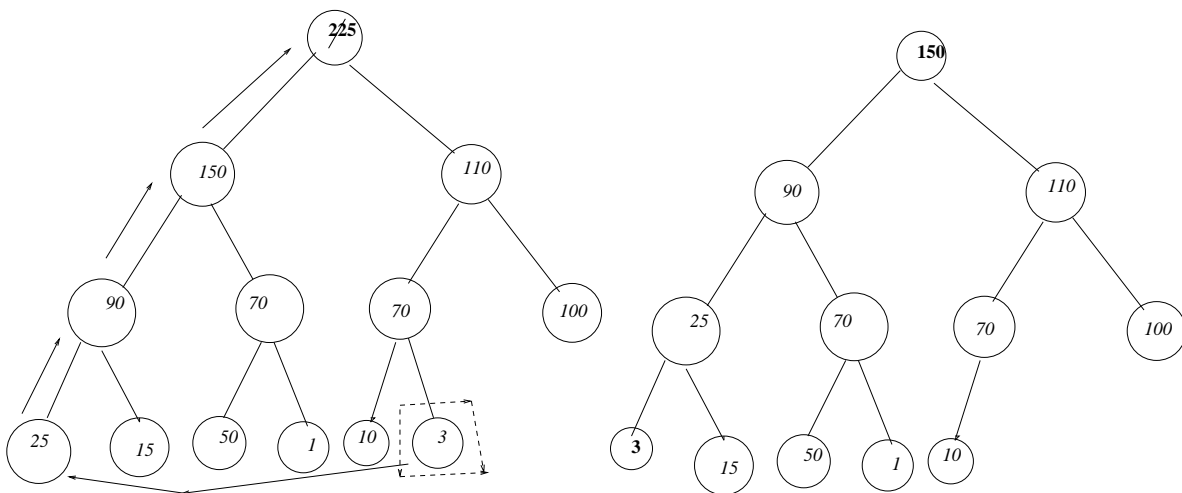
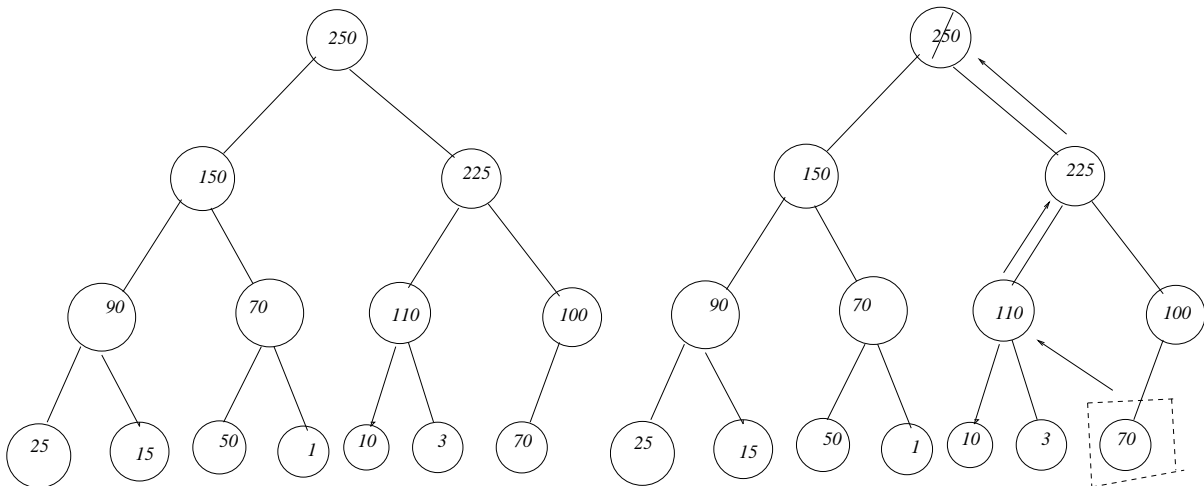
**Closed Book, closed note exam. Show your work! we must follow your reasoning. Give the best result that you can give! Over 100 points is bonus.**

SIGNATURE .....

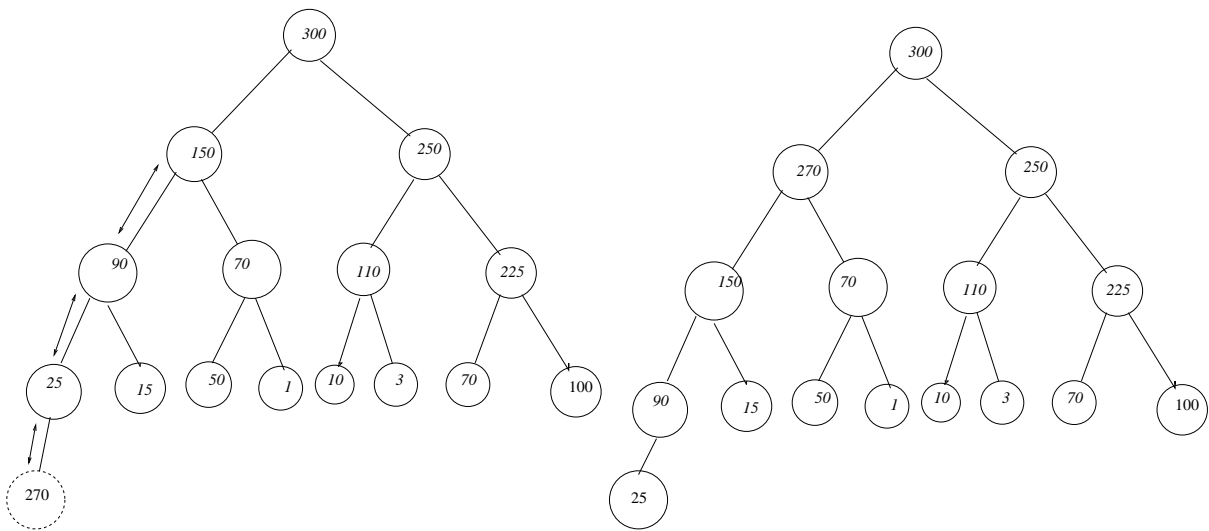
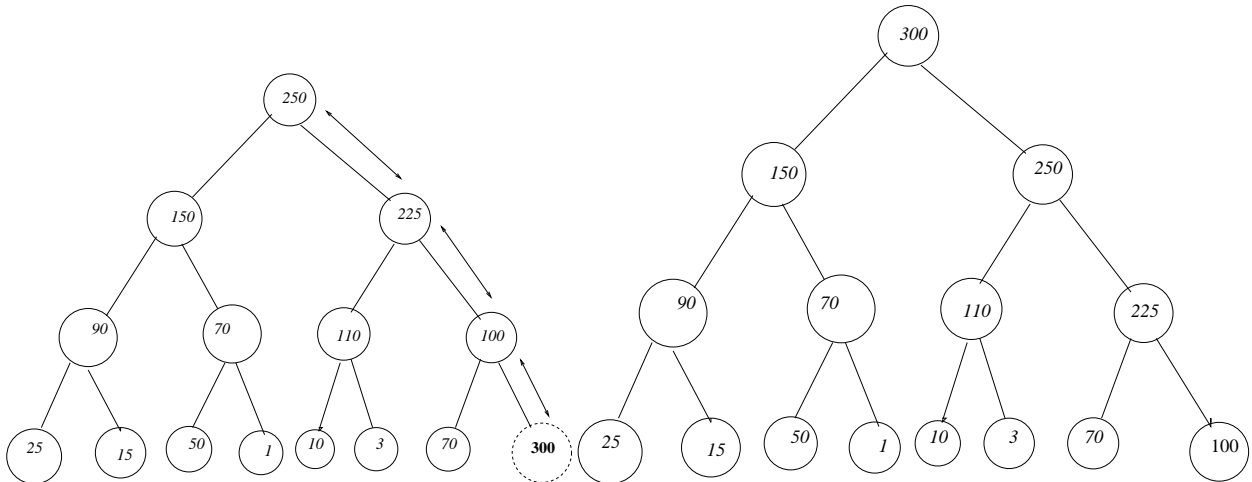
Time of Submission:

1. Given Heap  $H_o$ , apply successively:

apply twice deletemax operation to  $H_o$  (**5 pts** each)



i) insert 300, insert 270 successively ( **2 pts** )



2. **Hashing**. Let  $h(k) = k \bmod 17$  and  $h'_2(k) = k \bmod 11$  and  $h_2(k) = h'_2(k)$  if  $h'_2(k) > 0$ , and  $h_2(k) = 1$  otherwise. Let  $h(k, i) = (h_1(k) + ih_2(k)) \bmod 17$ . Using the sequence  $h(k, i)$   $i=0, 1, 2, \dots$  We want to place following in a Hash table: 40, 21, 4, 67, 31, 38, 37, 54, 6, 23, 7, 33, 50

**4 pts**

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16

Notation:  $h(k, i) = h_1(k) + ih_2(k) = t \mapsto A(t) = k$

First, let us compute  $h(k)$  for each  $k$ :

k	40	21	4	67	31	38	37	54	6	23	7	33	50
$h_1(k)$	6	4	4	16	14	4	3	3	6	6	7	16	16
$h_2(k)$	7	10	4	1	9	5	4	10	6	1	7	1	6
t	6	4	8	16	14	9	3	13	12	7	11	0	5

- $k=40 \ h_1(k) = 6, \mapsto A(6)=40$
- $k=21 \ h_1(k) = 4, \mapsto A(4)=21$
- $k=4 \ h_1(k) = 4 = h_2(k), 4 + 4 = t, i=1, \mapsto A(8)=4$
- $k=67 \ h_1(k) = 16, \mapsto A(16)=67$
- $k=31 \ h_1(k) = 14, \mapsto A(14)=31$
- $k=38 \ h_1(k) = 4, h_2(k) = 5, 4+5=t, i=1, \mapsto A(9)=38$
- $k=37 \ h_1(k) = 3, \mapsto A(3)=37$
- $k=54 \ h_1(k) = 3, h_2(k) = 10, 3+10=t, i=1, \mapsto A(13)=54$
- $k=6 \ h_1(k) = 6, h_2(k) = 6, 6+6=t, i=1, \mapsto A(12)=6$
- $k=23 \ h_1(k) = 6, h_2(k) = 1, 6+1=t, i=1, \mapsto A(7)=23$
- $k=7 \ h_1(k) = 7, h_2(k) = 7, 7, 14, 21=4, 11=t, i=3, \mapsto A(11)=7$
- $k=33 \ h_1(k) = 16, h_2(k) = 1, 16+1=0=t, i=1, \mapsto A(0)=33$
- $k=50 \ h_1(k) = 16, h_2(k) = 6, 16+6=5=t, i=1, \mapsto A(5)=50$

Thus we obtain the table:

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
33			37	21	50	40	23	4	38		7	6	54	31		67

– Solve the same input with  $h_1$  and linear probing

**2 pts**

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16

First, let us compute  $h(k)$  for each  $k$ :

k	40	21	4	67	31	38	37	54	6	23	7	33	50
$h(k)$	6	4	4	16	14	4	3	3	6	6	7	16	16

For each  $k$  if  $h(k)$  is empty, you place  $k$  at position  $h(k)$ , otherwise you increase  $h(k)$  by 1 in a circular fashion, until you find an empty spot.

In terms of double hashing  $h_2(k) = 1$  for each  $k$ .

Thus we obtain the table:

$k=40, h(k)=6, A(6)=40$

$k=21, h(k)=4, A(4)=21$

$k=4, h(k)=4, 4$  is full  $A(5)=4$

$k=67, h(k)=16, A(16)=67$

$k=31, h(k)=14, A(14)=31$

$k=38, h(k)=4, 4,5,6$  is full,  $A(7)=38$

$k=37, h(k)=3, A(3)=37$

$k=54, h(k)=3, 3,4,5,6,7$  is full,  $A(8)=54$

$k=6, h(k)=6, 6,7,8$  is full  $A(9)=6$

$k=23, h(k)=6, 6,7,8,9$  is full,  $A(10)=23$

$k=7, h(k)=7, 7,8,9,10$  is full,  $A(11)=7$

$k=33, h(k)=16, 16$  is full,  $A(0)=33$

$k=50, h(k)=16, 16, 0$  is full  $A(1)=50$

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
33	50		37	21	4	40	38	54	6	23	7			31		67